

$$V_\tau(\xi_k) = \min_{u_k, \dots, u_{k+\tau-1}} \mathbb{E} \left\{ \sum_{j=k}^{k+\tau-1} c(x_{j+1}, u_j) \mid \xi_k \right\}$$